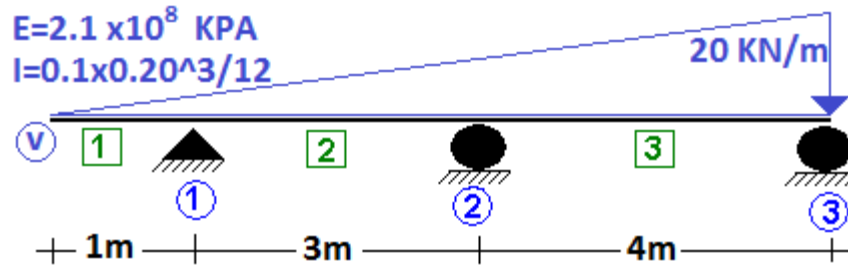


Encuentre las reacciones por el método de las Flexibilidades de la viga de la siguiente figura:

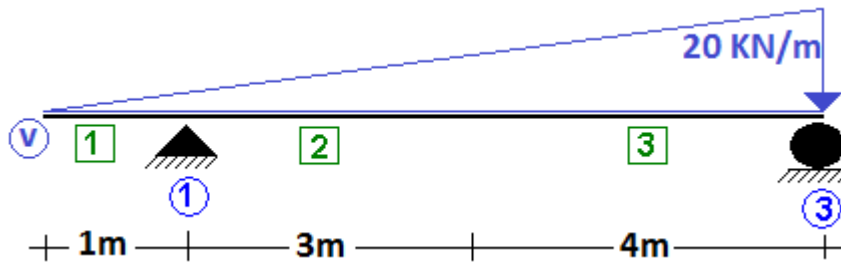


#1: [CaseMode := Sensitive, InputMode := Word]

#2:
$$\left[E := 2.1 \cdot 10^8, I := \frac{0.1 \cdot 0.2^3}{12} \right]$$

#3:
$$\left[E := 2.1 \cdot 10^8, I = 6.666666666 \cdot 10^{-5} \right]$$

Flexibilización de la estructura con reacciones y momentos flectores:



#4: [Rf1 :=, Rf3 :=]

#5:
$$\left[\begin{array}{l} Rf1 + Rf3 = \frac{20 \cdot 8}{2} \\ Rf1 \cdot 1 + Rf3 \cdot 8 = \frac{20 \cdot 8}{2} \cdot \frac{2}{3} \cdot 8 \end{array} \right]$$

#6:
$$\left[\left[Rf1 := \frac{640}{21}, Rf3 := \frac{1040}{21} \right] \right]$$

#7: [Rf1 = 30.47619047 ^ Rf3 = 49.52380952]

#8: [MF1(x) :=, MF23(x) :=, w(x) :=]

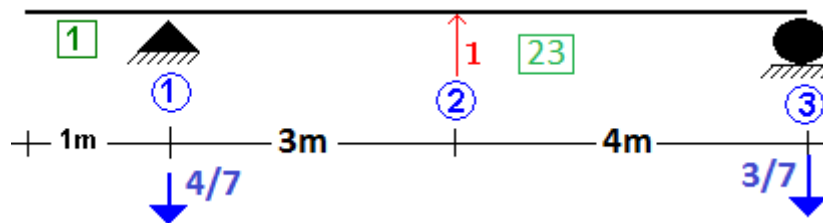
#9:
$$\left[\begin{array}{l} w(x) := \frac{20}{8} \cdot x \\ MF1(x) := - \frac{w(x) \cdot x}{2} \cdot \frac{1}{3} \cdot x \\ MF23(x) := - \frac{w(x) \cdot x}{2} \cdot \frac{1}{3} \cdot x + Rf1 \cdot (x - 1) \end{array} \right]$$

#10:
$$\left[\begin{array}{l} w(x) := \frac{5 \cdot x}{2} \\ MF1(x) := - \frac{5 \cdot x^3}{12} \\ MF23(x) := - \frac{5 \cdot (7 \cdot x^3 - 512 \cdot x + 512)}{84} \end{array} \right]$$

#11:
$$\left[\begin{array}{l} w(x) = 2.5 \cdot x \\ MF1(x) = - 0.4166666666 \cdot x^3 \\ MF23(x) = - 0.05952380952 \cdot (7 \cdot x^3 - 512 \cdot x + 512) \end{array} \right]$$

I) Deflexión de la viga flexibilizada:

Carga unitaria ficticia vertical hacia abajo en el nudo 2:



#12: [mf1(x) :=, mf2(x) :=, mf3(x) :=]

#13:

$$\begin{bmatrix} mf1(x) := 0 \\ mf2(x) := -\frac{4}{7} \cdot (x - 1) \\ mf3(x) := -\frac{4}{7} \cdot (x - 1) + 1 \cdot (x - 4) \end{bmatrix}$$

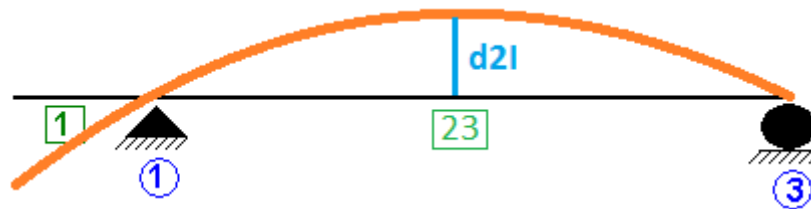
#14:

$$\begin{bmatrix} mf1(x) := 0 \\ mf2(x) := \frac{4}{7} - \frac{4 \cdot x}{7} \\ mf3(x) := \frac{3 \cdot x}{7} - \frac{24}{7} \end{bmatrix}$$

#15:

$$\begin{bmatrix} mf1(x) := 0 \\ mf2(x) := 0.5714285714 - 0.5714285714 \cdot x \\ mf3(x) := 0.4285714285 \cdot x - 3.428571428 \end{bmatrix}$$

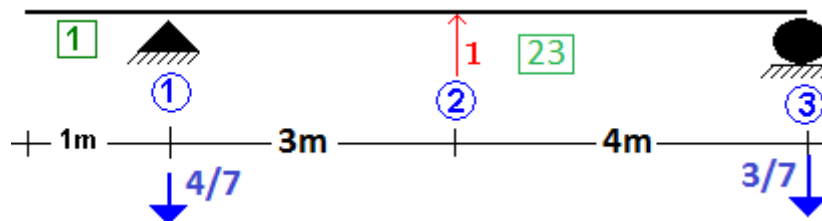
Aplicación del método de las Flexibilidades:

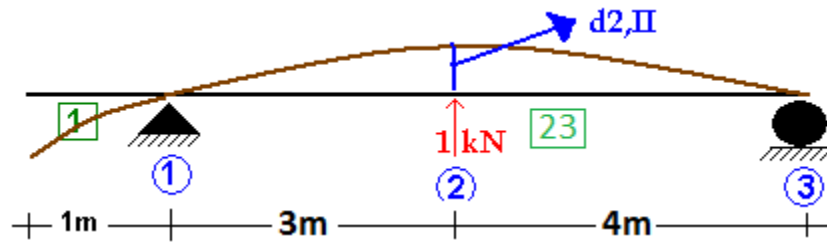


#16:
$$d2I := \frac{1}{E \cdot I} \cdot \left(\int_0^1 MF1(x) \cdot mf1(x) \, dx + \int_1^4 MF23(x) \cdot mf2(x) \, dx + \int_4^8 MF23(x) \cdot mf3(x) \, dx \right)$$

#17:
$$d2I := -0.02416241496$$

Carga unitaria ficticia para deflexión en el nudo 2 de la viga flexibilizada y cargada en el apoyo:





#18:
$$d2II := \frac{1}{E \cdot I} \cdot \left(\int_0^1 mf1(x) \cdot mf1(x) dx + \int_1^4 mf2(x) \cdot mf2(x) dx + \int_4^8 mf3(x) \cdot mf3(x) dx \right)$$

#19:
$$d2II := 0.0004897959183$$

Ecuación del método de las Flexibilidades para el apoyo 2:

#20: $[R2 :=]$

#21: $d2I + R2 \cdot d2II = 0$

#22: $R2 := 49.3315972$

Ecuaciones de la estática:

#23: $[R1 :=, R3 :=]$

#24:
$$\begin{bmatrix} R1 + R2 + R3 = \frac{20 \cdot 8}{2} \\ R1 \cdot 1 + R2 \cdot 4 + R3 \cdot 8 = \frac{20 \cdot 8}{2} \cdot \frac{2}{3} \cdot 8 \end{bmatrix}$$

#25: $[R1 = 2.286706361 \wedge R3 = 28.38169643]$

