



#1: [CaseMode := Sensitive, InputMode := Word]

Longitudes de cada elemento:

#2: 
$$\left[ L1 := 4, L2 := 3, L3 := \sqrt{4^2 + 3^2}, L4 := \sqrt{2^2 + 1^2 + 3^2}, L5 := \sqrt{2^2 + 1^2 + 3^2}, L6 := \sqrt{2^2 + 2^2 + 3^2} \right]$$

#3: 
$$\left[ L1 := 4, L2 := 3, L3 := 5, L4 := \sqrt{14}, L5 := \sqrt{14}, L6 := \sqrt{17} \right]$$

#4: 
$$\left[ L1 := 4, L2 := 3, L3 := 5, L4 := 3.741657386, L5 := 3.741657386, L6 := 4.123105625 \right]$$

Descomposición de la fuerza distribuida de 3KN/m:

#5: 
$$\left[ f_x := 3 \cdot \frac{2}{L5}, f_y := 3 \cdot \frac{-1}{L5}, f_z := 3 \cdot \frac{-3}{L5} \right]$$

#6: 
$$\left[ f_x := \frac{3 \cdot \sqrt{14}}{7}, f_y := -\frac{3 \cdot \sqrt{14}}{14}, f_z := -\frac{9 \cdot \sqrt{14}}{14} \right]$$

#7: 
$$\left[ f_x := 1.603567451, f_y := -0.8017837257, f_z := -2.405351177 \right]$$

Equilibrio estático externo:

$\sum F_x=0, \sum F_y=0, \sum F_z=0$

$\sum M$  respecto al nudo 4=0

#8:  $[X1 :=, X3 :=, Y1 :=, Z1 :=, Z2 :=, Z3 :=]$

$$\begin{bmatrix} X1 + X3 + fx \cdot L5 + 5 \cdot \frac{3}{5} = 0 \\ Y1 + fy \cdot L5 = 0 \\ Z1 + Z2 + Z3 + fz \cdot L5 + 5 \cdot \frac{4}{5} = 0 \\ + Y1 \cdot 3 - Z1 \cdot 1 - Z2 \cdot 1 + Z3 \cdot 2 = 0 \\ - X1 \cdot 3 - X3 \cdot 3 + Z1 \cdot 2 - Z2 \cdot 2 - Z3 \cdot 2 = 0 \\ + X1 \cdot 1 - X3 \cdot 2 - Y1 \cdot 2 = 0 \end{bmatrix}$$

#10:  $\left[ X1 := -4, X3 := -5, Y1 := 3, Z1 := -\frac{17}{4}, Z2 := \frac{127}{12}, Z3 := -\frac{4}{3} \right]$

#11:  $[X1 = -4 \wedge X3 = -5 \wedge Y1 = 3 \wedge Z1 = -4.25 \wedge Z2 = 10.58333333 \wedge Z3 = -1.333333333]$

**Cálculo de las fuerzas internas en los nudos:**

Procedimiento:

nudo:  $n \sum F_{internas} = \sum F_{externas}$ ,

elemento:  $e \sum F=0; \sum M=0$

Secuencia:

- n1
- e1
- e3
- e4
- n2
- e5
- e2
- n3
- e6

Chequeo n4

#12:  $[f12 :=, f21 :=, f23 :=, f32 :=, f13 :=, f31 :=, f14 :=, f41 :=, f24 :=, f42 :=, f34 :=, f43 :=]$

Nudo 1:

$$\#13: \begin{bmatrix} -f_{12} - f_{13} \cdot \frac{4}{L3} - f_{14} \cdot \frac{2}{L4} = X1 \\ -f_{13} \cdot \frac{3}{L3} - f_{14} \cdot \frac{1}{L4} = Y1 \\ -f_{14} \cdot \frac{3}{L4} = Z1 \end{bmatrix}$$

Elementos 1, 3 y 4:

$$\#14: \begin{bmatrix} -f_{12} + f_{21} = 0 \\ -f_{13} + f_{31} = 0 \\ -f_{14} + f_{41} = 0 \end{bmatrix}$$

Nudo 2:

$$\#15: \begin{bmatrix} f_{21} + f_{24} \cdot \frac{2}{L5} = 0 \\ -f_{23} - f_{24} \cdot \frac{1}{L5} = 0 \end{bmatrix}$$

Elementos 5 y 2:

$$\#16: \begin{bmatrix} f_{42} - 3 \cdot L5 - f_{24} = 0 \\ -f_{23} + f_{32} = 0 \end{bmatrix}$$

Nudo 3:

$$\#17: \left[ f_{31} \cdot \frac{4}{L3} + f_{34} \cdot \frac{2}{L6} = X3 \right]$$

Elemento 6:

$$\#18: [-f_{43} + f_{34} = 0]$$

#19:

$$\left[ \begin{array}{ccc} f_{12} := \frac{127}{18} & f_{13} := -\frac{265}{36} & f_{14} := \frac{17 \cdot \sqrt{14}}{12} \\ f_{21} := \frac{127}{18} & f_{23} := \frac{127}{36} & f_{24} := -\frac{127 \cdot \sqrt{14}}{36} \\ f_{31} := -\frac{265}{36} & f_{32} := \frac{127}{36} & f_{34} := \frac{4 \cdot \sqrt{17}}{9} \\ f_{41} := \frac{17 \cdot \sqrt{14}}{12} & f_{42} := -\frac{19 \cdot \sqrt{14}}{36} & f_{43} := \frac{4 \cdot \sqrt{17}}{9} \end{array} \right]$$

#20:

$$\left[ \begin{array}{ccc} f_{12} := 7.055555555 & f_{13} := -7.361111111 & f_{14} := 5.300681297 \\ f_{21} := 7.055555555 & f_{23} := 3.527777777 & f_{24} := -13.19973578 \\ f_{31} := -7.361111111 & f_{32} := 3.527777777 & f_{34} := 1.832491389 \\ f_{41} := 5.300681297 & f_{42} := -1.97476362 & f_{43} := 1.832491389 \end{array} \right]$$

Chequeo nudo 4:

#21:

$$\left[ \begin{array}{l} f_{41} \cdot \frac{2}{L4} - f_{42} \cdot \frac{2}{L5} - f_{43} \cdot \frac{2}{L6} = 5 \cdot \frac{3}{5} \\ f_{41} \cdot \frac{1}{L4} + f_{42} \cdot \frac{1}{L5} - f_{43} \cdot \frac{2}{L6} = 0 \\ f_{41} \cdot \frac{3}{L4} + f_{42} \cdot \frac{3}{L5} + f_{43} \cdot \frac{3}{L6} = 5 \cdot \frac{4}{5} \end{array} \right]$$

#22:

$$\left[ \begin{array}{l} 3 = 3 \\ 0 = 0 \\ 4 = 4 \end{array} \right]$$