

Resolver la deformación y esfuerzo del ejercicio con aproximación cuadrática:

#1: [CaseMode := Sensitive, InputMode := Word]

#2: $u(x) := a_1 + a_2 \cdot x + a_3 \cdot x^2$

#3:
$$\begin{bmatrix} u(0) = 0 \\ u(2) = 0 \end{bmatrix}$$

#4:
$$\begin{bmatrix} a_1 = 0 \\ a_1 + 2 \cdot a_2 + 4 \cdot a_3 = 0 \end{bmatrix}$$

#5:
$$\text{SOLVE} \left(\begin{bmatrix} a_1 = 0 \\ a_1 + 2 \cdot a_2 + 4 \cdot a_3 = 0 \end{bmatrix}, [a_1, a_2] \right)$$

#6: $[a_1 = 0 \wedge a_2 = -2 \cdot a_3]$

#7: $u(x) := 0 + (-2 \cdot a_3) \cdot x + a_3 \cdot x^2$

#8: $u(x) := a_3 \cdot x^2 - 2 \cdot a_3 \cdot x$

Energía potencial total:

#9:
$$\Pi = \frac{1}{2} \cdot \int_0^2 A \cdot E \cdot \left(\frac{d}{dx} u(x) \right)^2 dx - 2 \cdot u(1)$$

$$\#10: \quad \Pi = \frac{1}{2} \cdot \int_0^2 \left(\frac{d}{dx} u(x) \right)^2 dx - 2 \cdot u(1)$$

$$\#11: \quad \Pi = \frac{4 \cdot a^3}{3} + 2 \cdot a^3$$

Minimización de la energía potencial:

$$\#12: \quad \frac{d}{da^3} \left(\frac{4 \cdot a^3}{3} + 2 \cdot a^3 \right) = 0$$

$$\#13: \quad \text{SOLVE} \left(\frac{d}{da^3} \left(\frac{4 \cdot a^3}{3} + 2 \cdot a^3 \right) = 0, a^3 \right)$$

$$\#14: \quad a^3 = - \frac{3}{4}$$

$$\#15: \quad u(x) := 0 + \left(-2 \cdot \left(- \frac{3}{4} \right) \right) \cdot x + \left(- \frac{3}{4} \right) \cdot x^2$$

$$\#16: \quad u(x) := \frac{3 \cdot x}{2} - \frac{3 \cdot x^2}{4}$$

$$\#17: \quad u_1 = u(1)$$

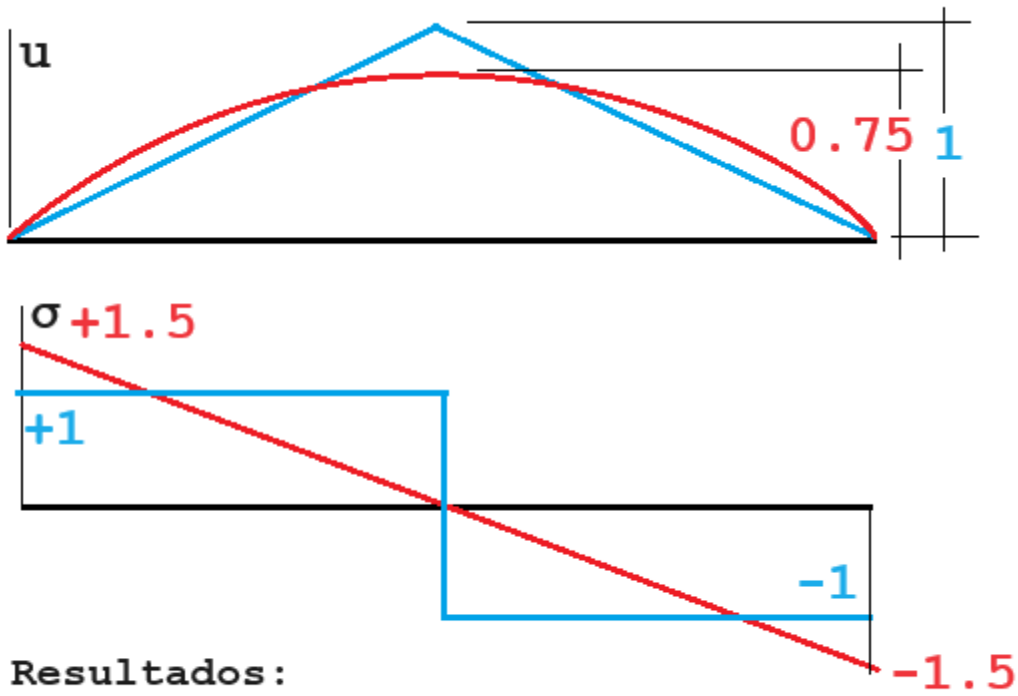
$$\#18: \quad u_1 = \frac{3}{4}$$

Esfuerzo axial puro:

$$\#19: \quad \sigma(x) := E \cdot \frac{d}{dx} u(x)$$

$$\#20: \quad \sigma(x) := 1 \cdot \frac{d}{dx} u(x)$$

$$\#21: \quad \sigma(x) := 1.5 \cdot (1 - x)$$



Resultados:

Mecánica de materiales

Aproximación polinómica