

Coordenadas (m)			
Nodo	X	Y	Z
1	0	0	0
2	6	0	0
3	6	3	0
4	4	0	5

#1: [CaseMode := Sensitive, InputMode := Word]

**Longitud de los elementos:**

#2:  $[L_1 := 6, L_2 := \sqrt{4^2 + 5^2}, L_3 := \sqrt{2^2 + 5^2}, L_4 := 3, L_5 := \sqrt{2^2 + 3^2 + 5^2}, L_6 := \sqrt{6^2 + 3^2}]$

#3:  $[L_1 := 6, L_2 := 6.403124237, L_3 := 5.385164807, L_4 := 3, L_5 := 6.164414002, L_6 := 6.708203932]$

#4:  $[L_1 := 6, L_2 := \sqrt{41}, L_3 := \sqrt{29}, L_4 := 3, L_5 := \sqrt{38}, L_6 := 3\sqrt{5}]$

**Equilibrio estático con el Diagrama de cuerpo Libre (DCL) de la estructura completa:**

#5:  $[X_1 :=, Y_1 :=, Z_1 :=, Y_2 :=, Z_2 :=, Z_3 :=]$

 **$\sum F=0$  y  $\sum M$  respecto al nudo 1=0**

$$X_1 + 4 \cdot L_5 \cdot \frac{2}{L_5} - 5 = 0$$

$$Y_1 + Y_2 + 6 + 4 \cdot L_5 \cdot \frac{3}{L_5} = 0$$

$$Z_1 + Z_2 + Z_3 - 4 \cdot L_5 \cdot \frac{5}{L_5} = 0$$

#6:

$$Z_3 \cdot 3 - 6 \cdot 5 - 4 \cdot L_5 \cdot \frac{3}{L_5} \cdot 2.5 - 4 \cdot L_5 \cdot \frac{5}{L_5} \cdot 1.5 = 0$$

$$- Z_2 \cdot 6 - Z_3 \cdot 6 - 5 \cdot 5 + 4 \cdot L_5 \cdot \frac{2}{L_5} \cdot 2.5 + 4 \cdot L_5 \cdot \frac{5}{L_5} \cdot (4 + 1) = 0$$

$$Y_2 \cdot 6 + 6 \cdot 4 - 4 \cdot L_5 \cdot \frac{2}{L_5} \cdot 1.5 + 4 \cdot L_5 \cdot \frac{3}{L_5} \cdot (4 + 1) = 0$$

#7:  $[X_1 = -3 \wedge Y_1 = -6 \wedge Y_2 = -12 \wedge Z_1 = 4.166666666 \wedge Z_2 = -14.16666666 \wedge Z_3 = 30]$

#8:  $\left[ X_1 := -3, Y_1 := -6, Y_2 := -12, Z_1 := \frac{25}{6}, Z_2 := -\frac{85}{6}, Z_3 := 30 \right]$

**Otra forma:  $\sum F=0$  y  $\sum M$  respecto al nudo 4=0**

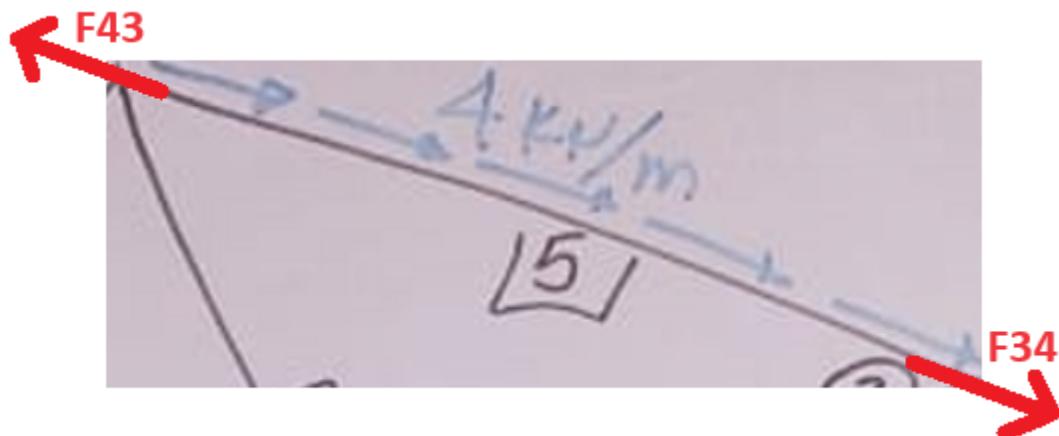
$$\left[ \begin{array}{l} X_1 + 4 \cdot L_5 \cdot \frac{2}{L_5} - 5 = 0 \\ Y_1 + Y_2 + 6 + 4 \cdot L_5 \cdot \frac{3}{L_5} = 0 \\ \#9: Z_1 + Z_2 + Z_3 - 4 \cdot L_5 \cdot \frac{5}{L_5} = 0 \\ Y_1 \cdot 5 + Y_2 \cdot 5 + Z_3 \cdot 3 = 0 \\ - X_1 \cdot 5 + Z_1 \cdot 4 - Z_2 \cdot 2 - Z_3 \cdot 2 = 0 \\ - Y_1 \cdot 4 + Y_2 \cdot 2 = 0 \end{array} \right]$$

$$\#10: \left[ X_1 = -3 \wedge Y_1 = -6 \wedge Y_2 = -12 \wedge Z_1 = \frac{25}{6} \wedge Z_2 = -\frac{85}{6} \wedge Z_3 = 30 \right]$$

$$\#11: [X_1 = -3 \wedge Y_1 = -6 \wedge Y_2 = -12 \wedge Z_1 = 4.166666666 \wedge Z_2 = -14.16666666 \wedge Z_3 = 30]$$

### DCL de los elementos:

DCL del elemento 5:



$$\#12: -F_{43} + 4 \cdot L_5 + F_{34} = 0$$

$$\#13: F_{43} := +4 \cdot L_5 + F_{34}$$

### DCL de los demás elementos:

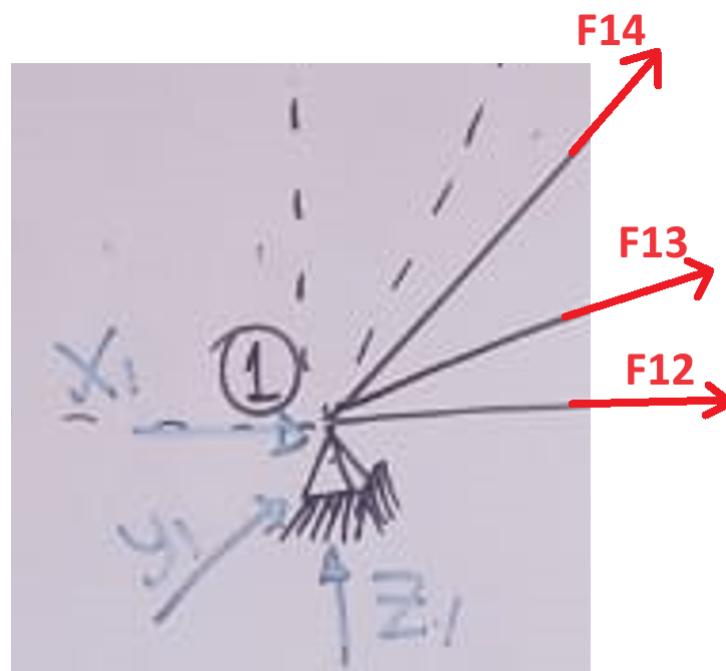
$$\#14: [F_{12} :=, F_{13} :=, F_{14} :=, F_{23} :=, F_{24} :=, F_{34} :=]$$



$$\#15: [F_{21} := F_{12}, F_{31} := F_{13}, F_{32} := F_{23}, F_{41} := F_{14}, F_{42} := F_{24}]$$

### DCL de los nudos:

Equilibrio del DCL del nudo 1:

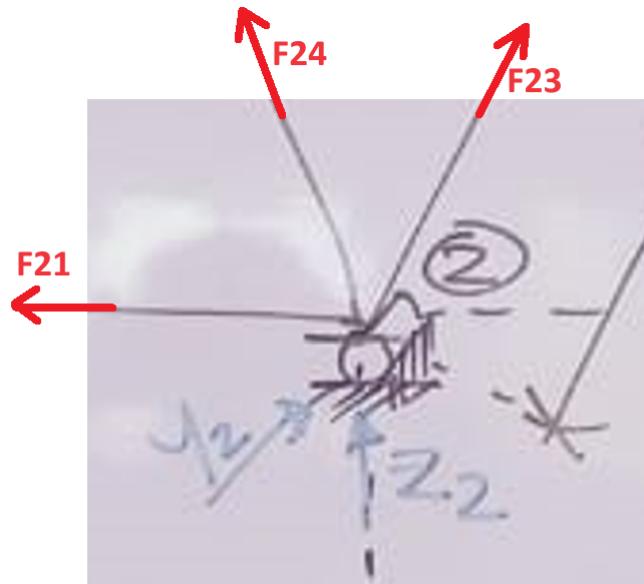


$$\#16: \begin{bmatrix} X_1 + F_{12} + F_{13} \cdot \frac{6}{L_6} + F_{14} \cdot \frac{4}{L_2} = 0 \\ Y_1 + F_{13} \cdot \frac{3}{L_6} = 0 \\ Z_1 + F_{14} \cdot \frac{5}{L_2} = 0 \end{bmatrix}$$

$$\#17: [F_{12} = -5.6666666666 \wedge F_{13} = 13.41640786 \wedge F_{14} = -5.335936864]$$

$$\#18: \left[ F_{12} := -\frac{17}{3}, F_{13} := 6\sqrt{5}, F_{14} := -\frac{5\sqrt{41}}{6} \right]$$

**Equilibrio en el DCL del nudo 2:**

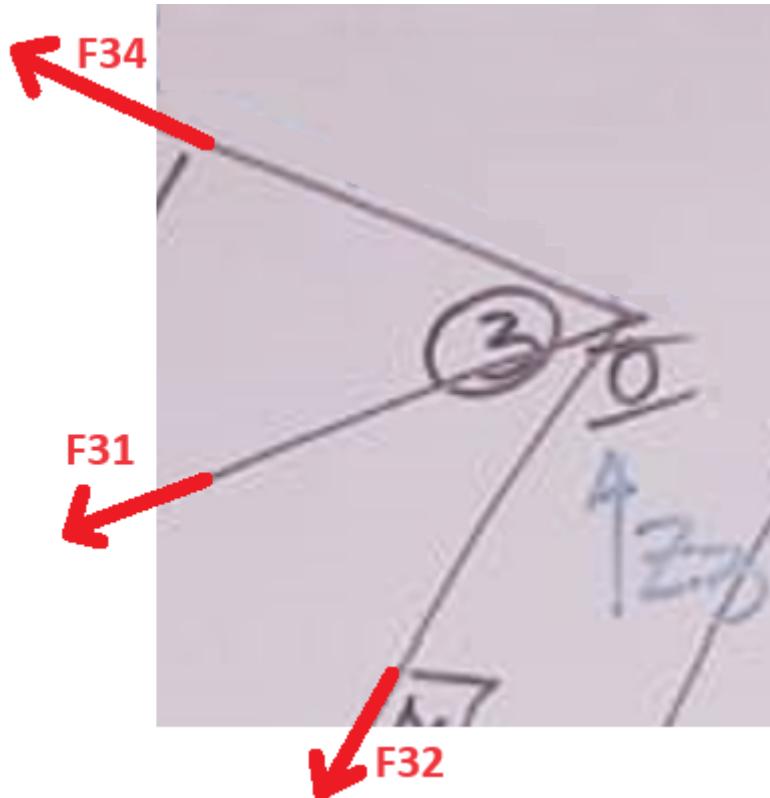


$$\begin{array}{l} \left[ \begin{array}{l} -F_{21} - F_{24} \cdot \frac{2}{L_3} = 0 \\ Y_2 + F_{23} = 0 \\ Z_2 + F_{24} \cdot \frac{5}{L_3} = 0 \end{array} \right] \\ \hline \end{array}$$

#20:  $[F_{23} = 12 \wedge F_{24} = 15.25796695]$

$$\begin{array}{l} \left[ \begin{array}{l} F_{23} := 12, F_{24} := \frac{17\sqrt{29}}{6} \end{array} \right] \\ \hline \end{array}$$

**Equilibrio en el DCL del nudo 3:**



$$\begin{array}{l} \left[ \begin{array}{l} -F_{31} \cdot \frac{6}{L_6} - F_{34} \cdot \frac{2}{L_5} = 0 \\ -F_{31} \cdot \frac{3}{L_6} - F_{32} - F_{34} \cdot \frac{3}{L_5} = 0 \\ Z_3 + F_{34} \cdot \frac{5}{L_5} = 0 \end{array} \right] \\ \hline \end{array}$$

#23:  $[F_{34} = -36.98648401]$

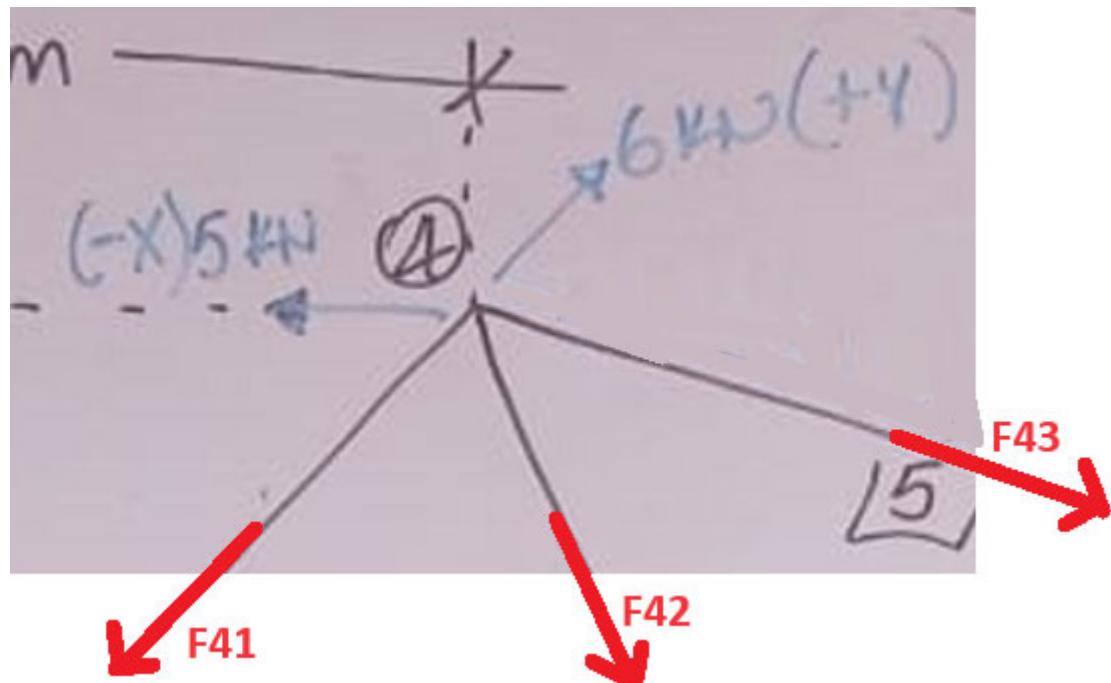
#24:  $[F_{34} := -6\sqrt{38}]$

**Del elemento 5:**

#25:  $F_{43} := -2\sqrt{38}$

#26:  $F_{43} := -12.328828$

**Equilibrio del nudo 4 para chequeo:**



#27:

$$\left[ \begin{array}{l} -F41 \cdot \frac{4}{L2} + F42 \cdot \frac{2}{L3} + F43 \cdot \frac{2}{L5} - 5 = 0 \\ F43 \cdot \frac{3}{L5} + 6 = 0 \\ -F41 \cdot \frac{5}{L2} - F42 \cdot \frac{5}{L3} - F43 \cdot \frac{5}{L5} = 0 \end{array} \right]$$

#28:

$$\begin{bmatrix} \text{true} \\ \text{true} \\ \text{true} \end{bmatrix}$$