

#1: [CaseMode := Sensitive, InputMode := Word]

#2: [Y1 :=, Y2 :=, W :=, L :=, E :=, I1 :=, I2 := 2·I1]

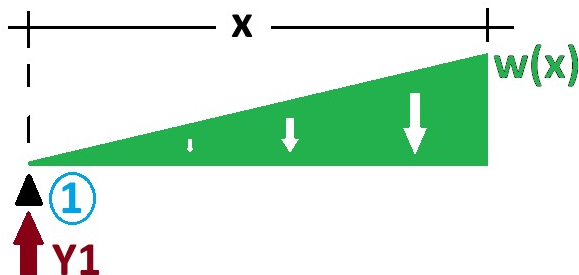
#3: [MF(x) :=, w(x) :=, δ1(x) :=, δ2(x) :=, δ12 :=, θ1 :=, θ12 :=]

Ecuaciones del equilibrio estático:

#4:
$$\begin{bmatrix} Y1 + Y2 - \frac{W \cdot L}{2} = 0 \\ Y2 \cdot L - \frac{W \cdot L}{2} \cdot \frac{2}{3} \cdot L = 0 \end{bmatrix}$$

#5:
$$\left[Y1 := \frac{L \cdot W}{6}, Y2 := \frac{L \cdot W}{3} \right]$$

Ecuación del diagrama de momento flector:

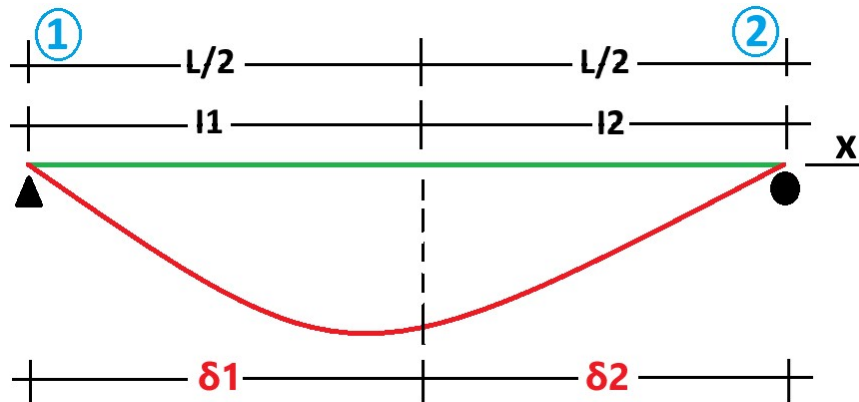


#6:
$$w(x) := \frac{W}{L} \cdot x$$

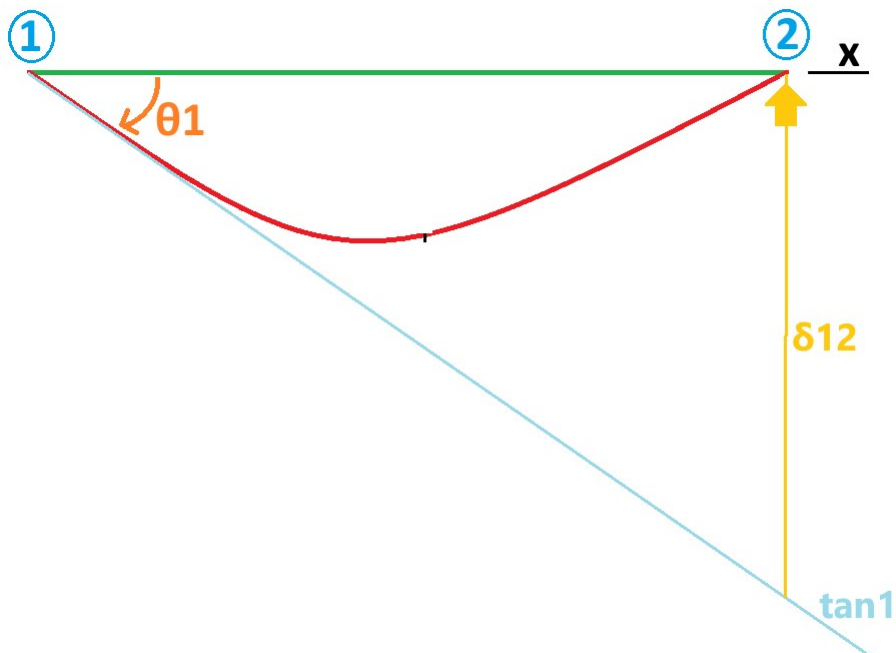
#7:
$$MF(x) := Y1 \cdot x - \frac{w(x) \cdot x}{2} \cdot \frac{x}{3}$$

#8:
$$MF(x) := \frac{L \cdot W \cdot x}{6} - \frac{W \cdot x^3}{6 \cdot L}$$

Curva elástica estimada (sin escala):



δ_{12} : Distancia entre la tangente en el punto 1 de la curva elástica al punto 2 de la curva elástica:



#9:
$$\delta_{12} := \frac{1}{E \cdot I1} \cdot \int_0^{L/2} MF(x) \cdot (L - x) \, dx + \frac{1}{E \cdot I2} \cdot \int_{L/2}^L MF(x) \cdot (L - x) \, dx$$

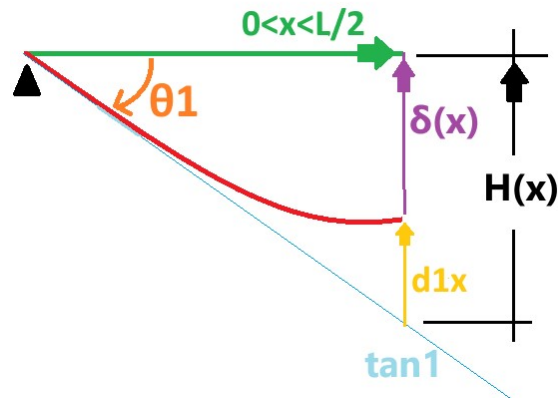
#10:
$$\delta_{12} := \frac{61 \cdot L^4 \cdot W}{3840 \cdot E \cdot I1}$$

Giro del punto 1 (estamos en el campo de pequeñas deformaciones, donde $TAN(\theta)=\theta$):

#11:
$$\theta_1 := - \frac{\delta_{12}}{L}$$

#12:
$$\theta_1 := - \frac{61 \cdot L^3 \cdot W}{3840 \cdot E \cdot I1}$$

Deformación por desplazamiento en un punto $0 < x < (L/2)$:



#13:
$$H(x) := (-\theta_1) \cdot x$$

#14:
$$H(x) := \frac{61 \cdot L^3 \cdot W \cdot x}{3840 \cdot E \cdot I1}$$

Se usa temporalmente la variable J para referirse a la variable x

#15:
$$d1J = \frac{1}{E \cdot I1} \cdot \int_0^J MF(x) \cdot (J - x) dx$$

#16:
$$d1J = \frac{J^3 \cdot W \cdot (10 \cdot L^2 - 3 \cdot J^2)}{360 \cdot E \cdot I1 \cdot L}$$

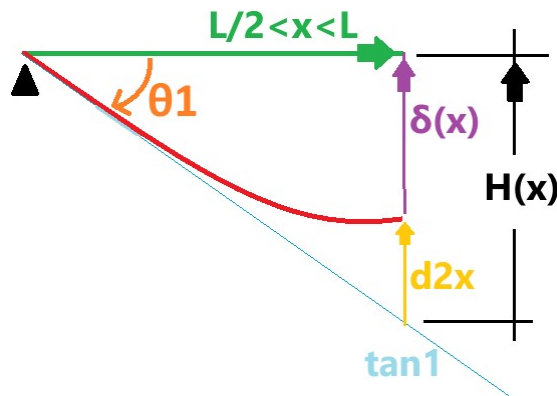
$$\#17: \text{SUBST} \left(d1J = \frac{J^3 \cdot W \cdot (10 \cdot L^2 - 3 \cdot J^2)}{360 \cdot E \cdot I1 \cdot L}, [d1J, J], [d1x, x] \right)$$

$$\#18: d1x := \frac{W \cdot x^3 \cdot (10 \cdot L^2 - 3 \cdot x^2)}{360 \cdot E \cdot I1 \cdot L}$$

$$\#19: \delta1(x) := H(x) - d1x$$

$$\#20: \delta1(x) := \frac{W \cdot x \cdot (96 \cdot x^4 - 320 \cdot L^2 \cdot x^2 + 183 \cdot L^4)}{11520 \cdot E \cdot I1 \cdot L}$$

Deformación por desplazamiento en un punto $(L/2) < x < L$:



$$\#21: d2J = \frac{1}{E \cdot I1} \cdot \int_0^{L/2} MF(x) \cdot (J - x) \, dx + \frac{1}{E \cdot I2} \cdot \int_{L/2}^J MF(x) \cdot (J - x) \, dx$$

$$\#22: d2J = - \frac{W \cdot (48 \cdot J^5 - 160 \cdot J^3 \cdot L^2 - 105 \cdot J \cdot L^4 + 34 \cdot L^5)}{11520 \cdot E \cdot I1 \cdot L}$$

$$\#23: \text{SUBST} \left(d2J = - \frac{W \cdot (48 \cdot J^5 - 160 \cdot J^3 \cdot L^2 - 105 \cdot J \cdot L^4 + 34 \cdot L^5)}{11520 \cdot E \cdot I1 \cdot L}, [d2J, J], [d2x, x] \right)$$

$$\#24: d2x := - \frac{W \cdot (48 \cdot x^5 - 160 \cdot L^2 \cdot x^3 - 105 \cdot L^4 \cdot x + 34 \cdot L^5)}{11520 \cdot E \cdot I1 \cdot L}$$

$$\#25: \delta2(x) := H(x) - d2x$$

$$\#26: \quad \delta_2(x) := \frac{W \cdot (24 \cdot x^5 - 80 \cdot L \cdot x^2 \cdot x^3 + 39 \cdot L^4 \cdot x^4 + 17 \cdot L^5)}{5760 \cdot E \cdot I_1 \cdot L}$$

Deformación en el centro de la luz:

$$\#27: \quad \left[\delta_1\left(\frac{L}{2}\right), \delta_2\left(\frac{L}{2}\right) \right]$$

$$\#28: \quad \left[\frac{109 \cdot L^4 \cdot W}{23040 \cdot E \cdot I_1}, \frac{109 \cdot L^4 \cdot W}{23040 \cdot E \cdot I_1} \right]$$

$$\#29: \quad \left[\frac{0.004730902777 \cdot L^4 \cdot W}{E \cdot I_1}, \frac{0.004730902777 \cdot L^4 \cdot W}{E \cdot I_1} \right]$$