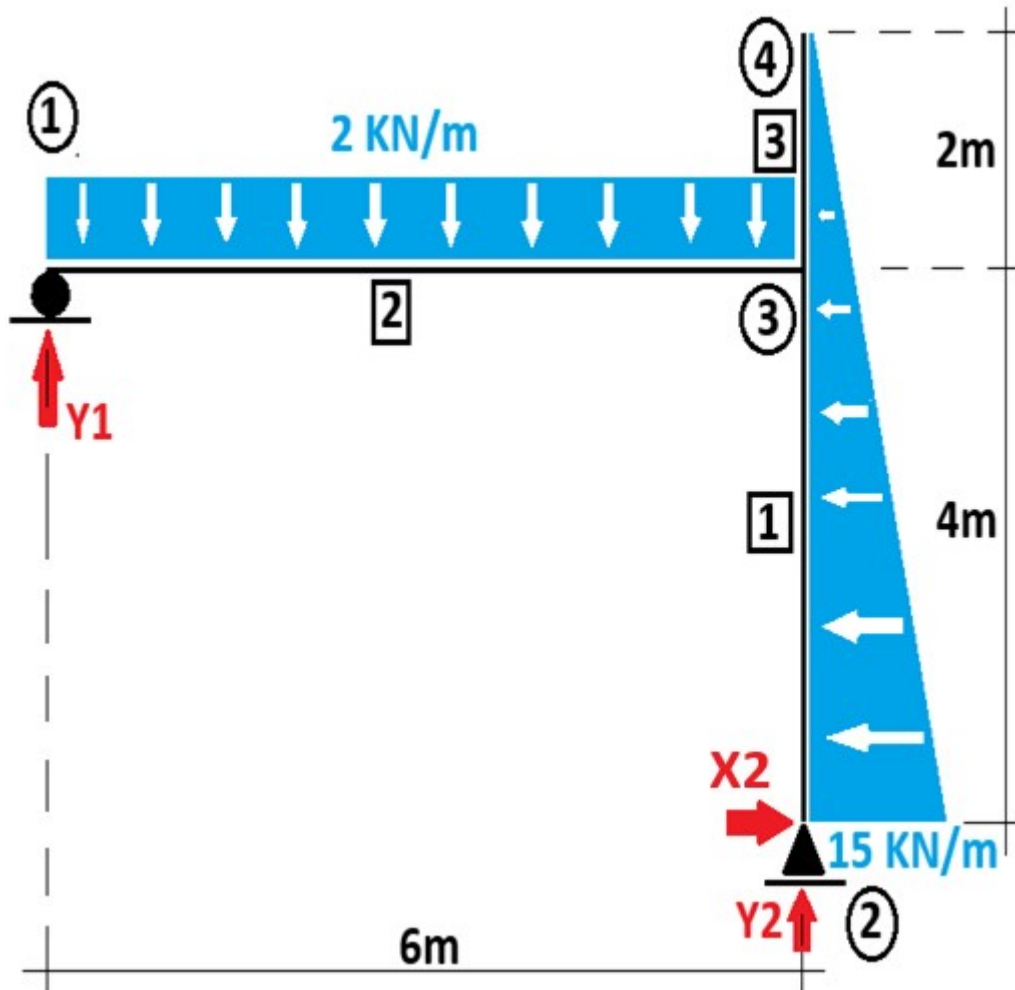


Resolver por el método de la Carga Unitaria Ficticia los desplazamientos del nudo 3:



#1: [CaseMode := Sensitive, InputMode := Word]

Datos del ejercicio:

$$\#2: \left[E := 2 \cdot 10^8, I_c := \frac{0.2^4}{12}, I_v := \frac{0.1^4}{12} \right]$$

#3: [y1 :=, x2 :=, y2 :=, x31 :=, y31 :=, m31 :=, x32 :=, y32 :=, m32 :=, MFv(x) :=, MFc1(x) :=, MFc2(x) :=]

Simplificación de expresiones con EI:

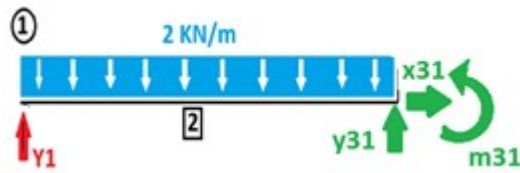
#4: [EIc := E · Ic, EIV := E · Iv]

Ecuaciones del equilibrio estático:

$$\#5: \begin{bmatrix} x_2 - \frac{15 \cdot 6}{2} = 0 \\ y_2 + y_1 - 2 \cdot 6 = 0 \\ -y_1 \cdot 6 + 2 \cdot 6 \cdot 3 + \frac{15 \cdot 6}{2} \cdot \frac{1}{3} \cdot 6 = 0 \end{bmatrix}$$

$$\#6: [x_2 := 45, y_1 := 21, y_2 := -9]$$

Diagramas de cuerpo libre de la viga:



$$\#7: \begin{bmatrix} y_1 + y_{31} - 2 \cdot 6 = 0 \\ x_{31} = 0 \\ y_{31} \cdot 6 - 2 \cdot 6 \cdot 3 + m_{31} = 0 \end{bmatrix}$$

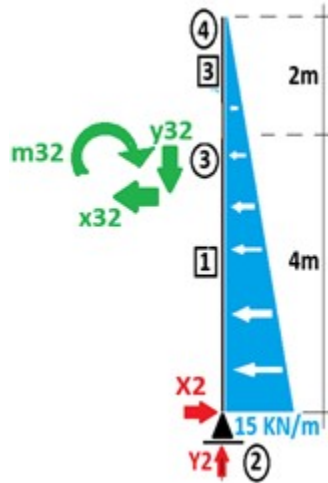
$$\#8: [m_{31} := 90, x_{31} := 0, y_{31} := -9]$$

Diagrama de cuerpo libre del nudo 3:



$$\#9: [x_{32} := x_{31}, y_{32} := y_{31}, m_{32} := m_{31}]$$

Chequeo de equilibrio con el diagrama de cuerpo libre de la columna:



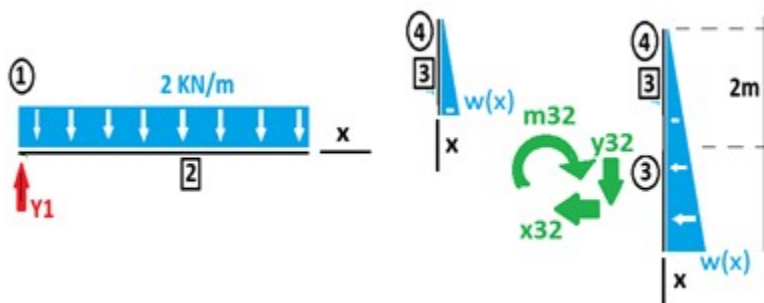
#10:

$$\begin{bmatrix} x_2 - x_{32} - \frac{15 \cdot 6}{2} = 0 \\ y_2 - y_{32} = 0 \\ -m_{32} + 15 \cdot \frac{6}{2} \cdot \frac{1}{3} \cdot 6 = 0 \end{bmatrix}$$

#11:

$$\begin{bmatrix} \text{true} \\ \text{true} \\ \text{true} \end{bmatrix}$$

Diagramas de momento flector de la estructura con las cargas originales MF(x):



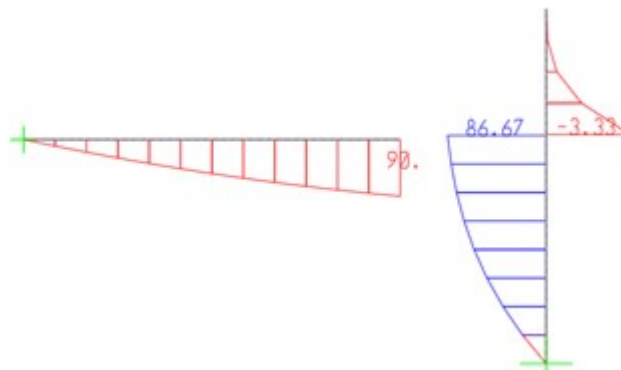
#12: $w(x) := \frac{15}{6} \cdot x$

#13:

$$\left[\begin{array}{l} MFv(x) := y1 \cdot x - \frac{2 \cdot x^2}{2} \\ MFc1(x) := - \frac{w(x) \cdot x}{2} \cdot \frac{1}{3} \cdot x \\ MFc2(x) := - \frac{w(x) \cdot x}{2} \cdot \frac{1}{3} \cdot x - x^3 \cdot 2 \cdot (x - 2) + m3 \cdot 2 \end{array} \right]$$

#14:

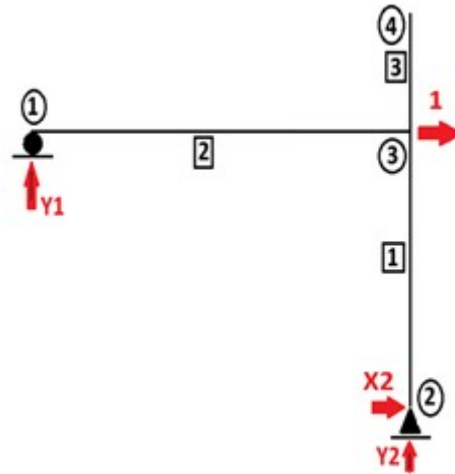
$$\left[\begin{array}{l} MFv(x) := 21 \cdot x - x^2 \\ MFc1(x) := - \frac{5 \cdot x^3}{12} \\ MFc2(x) := 90 - \frac{5 \cdot x^3}{12} \end{array} \right]$$



#15:

$$\left[\begin{array}{cc} MFv(0) & MFv(6) \\ MFc1(0) & MFc1(2) \\ MFc2(2) & MFc2(6) \end{array} \right] = \left[\begin{array}{cc} 0 & 90 \\ 0 & -3.333333333 \\ 86.66666666 & 0 \end{array} \right]$$

Estructura con la carga unitaria ficticia hacia la derecha en el nudo 3:



#16: $[y_{1f} :=, x_{2f} :=, y_{2f} :=, x_{31f} :=, y_{31f} :=, m_{31f} :=, x_{32f} :=, y_{32f} :=, m_{32f} :=, m_{fv}(x) :=,$
 $m_{fc1}(x) :=, m_{fc2}(x) :=]$

#17:
$$\begin{bmatrix} x_{2f} + 1 = 0 \\ y_{2f} + y_{1f} = 0 \\ -y_{1f} \cdot 6 - 1 \cdot 4 = 0 \end{bmatrix}$$

#18:
$$\left[x_{2f} := -1, y_{1f} := -\frac{2}{3}, y_{2f} := \frac{2}{3} \right]$$

Diagrama de cuerpo libre de la viga:



#19:
$$\begin{bmatrix} y_{1f} + y_{31f} = 0 \\ x_{31f} = 0 \\ -y_{1f} \cdot 6 + m_{31f} = 0 \end{bmatrix}$$

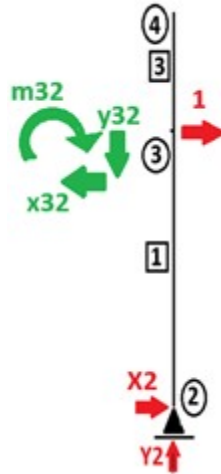
#20:
$$\left[m_{31f} := -4, x_{31f} := 0, y_{31f} := \frac{2}{3} \right]$$

Diagrama de cuerpo libre del nudo 3:



#21: [x32f := x31f, y32f := y31f, m32f := m31f]

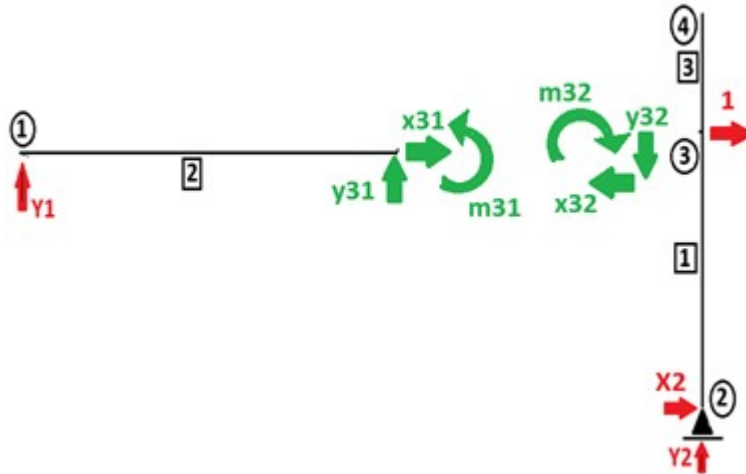
Diagrama de cuerpo libre de la columna para chequeo de equilibrio:



#22:
$$\begin{bmatrix} x2f - x32f + 1 = 0 \\ y2f - y32f = 0 \\ -m32f - 1 \cdot 4 = 0 \end{bmatrix}$$

#23:
$$\begin{bmatrix} \text{true} \\ \text{true} \\ \text{true} \end{bmatrix}$$

Momentos flectores de la estructura, cargada con la carga unitaria ficticia, usando los mismos ejes de coordenadas:



#24:

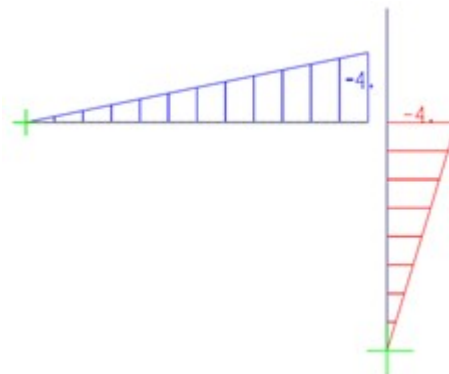
$$\begin{bmatrix} \text{mfV}(x) := y1f \cdot x \\ \text{mfc1}(x) := 0 \\ \text{mfc2}(x) := -x32f \cdot (x - 2) + 1 \cdot (x - 2) + m32f \end{bmatrix}$$

#25:

$$\begin{bmatrix} \text{mfV}(x) := -\frac{2 \cdot x}{3} \\ \text{mfc1}(x) := 0 \\ \text{mfc2}(x) := x - 6 \end{bmatrix}$$

#26:

$$\begin{bmatrix} \text{mfV}(x) := -0.6666666666 \cdot x \\ \text{mfc1}(x) := 0 \\ \text{mfc2}(x) := x - 6 \end{bmatrix}$$



#27:

$$\begin{bmatrix} \text{mfV}(0) & \text{mfV}(6) \\ \text{mfc1}(0) & \text{mfc1}(2) \\ \text{mfc2}(2) & \text{mfc2}(6) \end{bmatrix} = \begin{bmatrix} 0 & -4 \\ 0 & 0 \\ -4 & 0 \end{bmatrix}$$

Cálculo del desplazamiento del nudo 3, positivo hacia la derecha:

#28:
$$d3 = \frac{1}{EI_v} \cdot \int_0^6 \text{MFV}(x) \cdot \text{mfV}(x) \, dx + \frac{1}{EI_c} \cdot \int_0^2 \text{MFc1}(x) \cdot \text{mfc1}(x) \, dx + \frac{1}{EI_c} \cdot \int_2^6$$

$$\text{MFc2}(x) \cdot \text{mfc2}(x) \, dx$$

#29:
$$d3 = \frac{1}{EI_v} \cdot (-792) + \frac{1}{EI_c} \cdot 0 + \frac{1}{EI_c} \cdot \left(-\frac{1696}{3} \right)$$

#30:
$$d3 = -\frac{297}{625} + 0 + -\frac{53}{2500}$$

#31:
$$d3 = -0.4752 + 0 + -0.0212$$

#32:
$$d3 = -\frac{1241}{2500}$$

#33:
$$d3 = -0.4964$$

