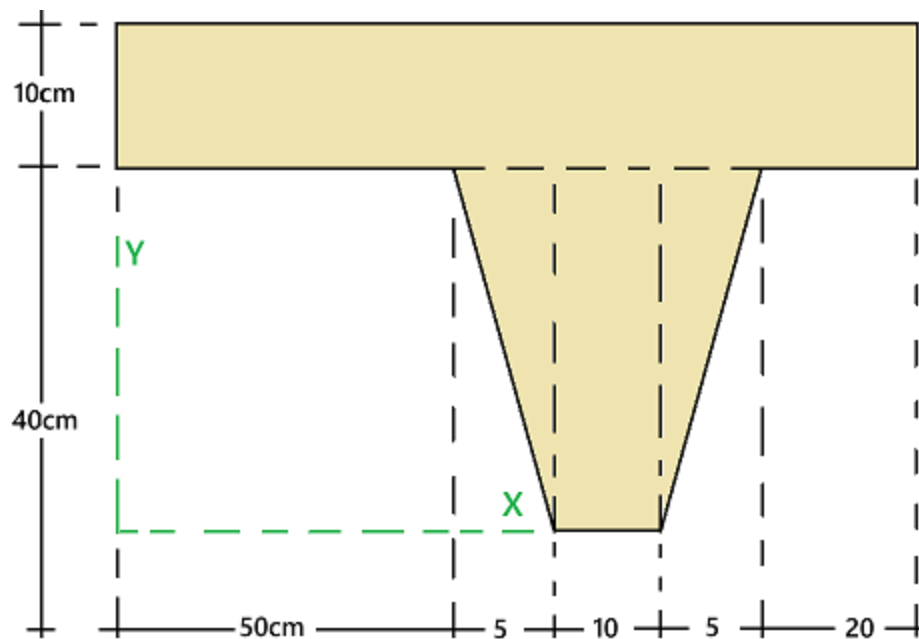
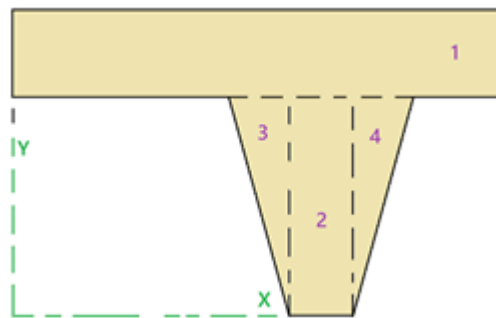


Encontrar las inercias centroidales máximas y mínimas por rotación:



#1: [CaseMode := Sensitive, InputMode := Word]

División por subáreas de formas geométricas conocidas:



Áreas individuales y total:

$$\begin{aligned} \#2: \quad & \left[A1 := (50 + 5 + 10 + 5 + 20) \cdot 10, A2 := 10 \cdot 40, A3 := \frac{5 \cdot 40}{2}, A4 := A3, A \right. \\ & \left. := A1 + A2 + A3 + A4 \right] \end{aligned}$$

#3: [A1 := 900, A2 := 400, A3 := 100, A4 := 100, A := 1500]

Centroides individuales respecto a los ejes X e Y:

#4:

$$\left[\begin{array}{ll} X_{cg1} := \frac{50 + 5 + 10 + 5 + 20}{2} & Y_{cg1} := 40 + \frac{10}{2} \\ X_{cg2} := 50 + 5 + \frac{10}{2} & Y_{cg2} := \frac{40}{2} \\ X_{cg3} := 50 + \frac{2}{3} \cdot 5 & Y_{cg3} := \frac{2}{3} \cdot 40 \\ X_{cg4} := 50 + 5 + 10 + \frac{1}{3} \cdot 5 & Y_{cg4} := Y_{cg3} \end{array} \right]$$

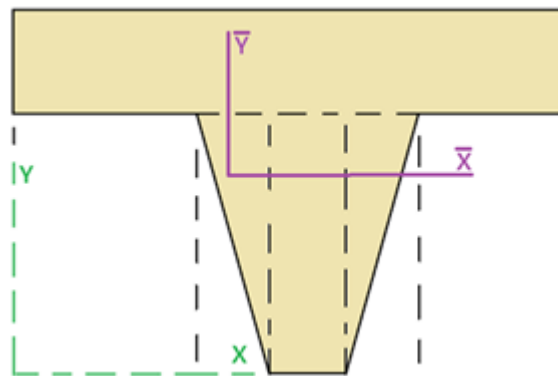
#5:

$$\left[\begin{array}{ll} X_{cg1} := 45 & Y_{cg1} := 45 \\ X_{cg2} := 60 & Y_{cg2} := 20 \\ X_{cg3} := \frac{160}{3} & Y_{cg3} := \frac{80}{3} \\ X_{cg4} := \frac{200}{3} & Y_{cg4} := \frac{80}{3} \end{array} \right]$$

#6:

$$\left[\begin{array}{ll} X_{cg1} := 45 & Y_{cg1} := 45 \\ X_{cg2} := 60 & Y_{cg2} := 20 \\ X_{cg3} := 53.33333333 & Y_{cg3} := 26.66666666 \\ X_{cg4} := 66.66666666 & Y_{cg4} := 26.66666666 \end{array} \right]$$

Centroide de la figura completa:



#7:

$$\left[X_{cg} := \frac{A1 \cdot X_{cg1} + A2 \cdot X_{cg2} + A3 \cdot X_{cg3} + A4 \cdot X_{cg4}}{A}, Y_{cg} := \right]$$

$$\left[\frac{A1 \cdot Y_{cg1} + A2 \cdot Y_{cg2} + A3 \cdot Y_{cg3} + A4 \cdot Y_{cg4}}{A} \right]$$

#8: $\left[X_{cg} := 51, Y_{cg} := \frac{323}{9} \right]$

#9: $[X_{cg} := 51, Y_{cg} := 35.888888888]$

Inercias centroidales individuales:

#10:
$$\left[\begin{array}{l} I_{xc1} := \frac{(50 + 5 + 10 + 5 + 20) \cdot 10^3}{12} \quad I_{yc1} := \\ I_{xc2} := \frac{10 \cdot 40^3}{12} \\ I_{xc3} := \frac{5 \cdot 40^3}{36} \\ I_{xc4} := I_{xc3} \end{array} \right]$$

$$\left[\begin{array}{l} \frac{(50 + 5 + 10 + 5 + 20) \cdot 10^3}{12} \quad I_{xyc1} := 0 \\ I_{yc2} := \frac{10 \cdot 40^3}{12} \quad I_{xyc2} := 0 \\ I_{yc3} := \frac{5 \cdot 40^3}{36} \quad I_{xyc3} := - \frac{5^2 \cdot 40^2}{72} \\ I_{yc4} := I_{yc3} \quad I_{xyc4} := \frac{5^2 \cdot 40^2}{72} \end{array} \right]$$

$$\#11: \begin{bmatrix} I_{xc1} := 7500 & I_{yc1} := 607500 & I_{xyc1} := 0 \\ I_{xc2} := \frac{160000}{3} & I_{yc2} := \frac{10000}{3} & I_{xyc2} := 0 \\ I_{xc3} := \frac{80000}{9} & I_{yc3} := \frac{1250}{9} & I_{xyc3} := -\frac{5000}{9} \\ I_{xc4} := \frac{80000}{9} & I_{yc4} := \frac{1250}{9} & I_{xyc4} := \frac{5000}{9} \end{bmatrix}$$

$$\#12: \begin{bmatrix} I_{xc1} := 7500 & I_{yc1} := 6.075 \cdot 10^5 & I_{xyc1} := 0 \\ I_{xc2} := 5.333333333 \cdot 10^4 & I_{yc2} := 3333.333333 & I_{xyc2} := 0 \\ I_{xc3} := 8888.888888 & I_{yc3} := 138.8888888 & I_{xyc3} := -555.5555555 \\ I_{xc4} := 8888.888888 & I_{yc4} := 138.8888888 & I_{xyc4} := 555.5555555 \end{bmatrix}$$

Inercias respecto a los ejes X e Y individuales:

$$\#13: \begin{bmatrix} I_{x1} := I_{xc1} + A1 \cdot Y_{cg1}^2 & I_{y1} := I_{yc1} + A1 \cdot X_{cg1}^2 & I_{xy1} := I_{xyc1} + \\ I_{x2} := I_{xc2} + A2 \cdot Y_{cg2}^2 & I_{y2} := I_{yc2} + A2 \cdot X_{cg2}^2 & I_{xy2} := I_{xyc2} + \\ I_{x3} := I_{xc3} + A3 \cdot Y_{cg3}^2 & I_{y3} := I_{yc3} + A3 \cdot X_{cg3}^2 & I_{xy3} := I_{xyc3} + \\ I_{x4} := I_{xc4} + A4 \cdot Y_{cg4}^2 & I_{y4} := I_{yc4} + A4 \cdot X_{cg4}^2 & I_{xy4} := I_{xyc4} + \\ A1 \cdot X_{cg1} \cdot Y_{cg1} \\ A2 \cdot X_{cg2} \cdot Y_{cg2} \\ A3 \cdot X_{cg3} \cdot Y_{cg3} \\ A4 \cdot X_{cg4} \cdot Y_{cg4} \end{bmatrix}$$

$$\#14: \begin{bmatrix} Ix1 := 1830000 & Iy1 := 2430000 & Ixy1 := 1822500 \\ Ix2 := \frac{640000}{3} & Iy2 := \frac{4330000}{3} & Ixy2 := 480000 \\ Ix3 := 80000 & Iy3 := \frac{853750}{3} & Ixy3 := \frac{425000}{3} \\ Ix4 := 80000 & Iy4 := \frac{1333750}{3} & Ixy4 := \frac{535000}{3} \end{bmatrix}$$

$$\#15: \begin{bmatrix} Ix1 := 1.83 \cdot 10^6 & Iy1 := 2.43 \cdot 10^6 \\ Ix2 := 2.133333333 \cdot 10^5 & Iy2 := 1.443333333 \cdot 10^6 \\ Ix3 := 8 \cdot 10^4 & Iy3 := 2.845833333 \cdot 10^5 \\ Ix4 := 8 \cdot 10^4 & Iy4 := 4.445833333 \cdot 10^5 \\ Ixy1 := 1.8225 \cdot 10^6 \\ Ixy2 := 4.8 \cdot 10^5 \\ Ixy3 := 1.416666666 \cdot 10^5 \\ Ixy4 := 1.783333333 \cdot 10^5 \end{bmatrix}$$

Inercias de toda la figura respecto a los ejes X e Y:

$$\#16: [Ix := Ix1 + Ix2 + Ix3 + Ix4, Iy := Iy1 + Iy2 + Iy3 + Iy4, Ixy := Ixy1 + Ixy2 + Ixy3 + Ixy4]$$

$$\#17: \left[Ix := \frac{2203333333}{10000}, Iy := \frac{11506249999}{2500}, Ixy := \frac{26224999999}{10000} \right]$$

$$\#18: [Ix := 2.203333333 \cdot 10^6, Iy := 4.602499999 \cdot 10^6, Ixy := 2.6225 \cdot 10^6]$$

Inercias centroidales de toda la figura:

$$\#19: \left[I_{xc} := I_x - A \cdot Y_{cg}^2, I_{yc} := I_y - A \cdot X_{cg}^2, I_{xyc} := I_{xy} - A \cdot X_{cg} \cdot Y_{cg} \right]$$

$$\#20: \left[I_{xc} := \frac{73254999991}{270000}, I_{yc} := \frac{1752499999}{2500}, I_{xyc} := -\frac{12300000001}{10000} \right]$$

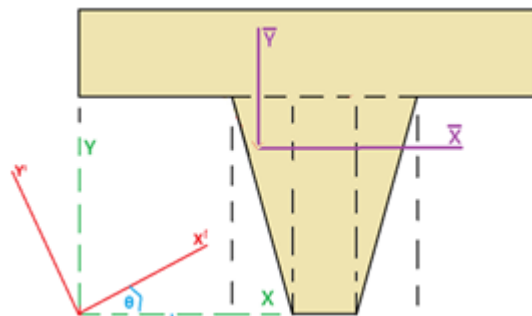
$$\#21: \left[I_{xc} := 2.713148147 \cdot 10^5, I_{yc} := 7.009999996 \cdot 10^5, I_{xyc} := -1.2300000001 \cdot 10^5 \right]$$

Ángulo donde se presentan las inercias principales, respecto a los ejes X e Y:

$$\#22: \theta := \frac{1}{2} \cdot \text{ATAN} \left(-\frac{2 \cdot I_{xy}}{I_x - I_y} \right)$$

$$\#23: \theta := 0.5708946404$$

Aproximadamente 33°



Inercias centroidales principales X' e Y':

$$\#24: \left[I_{max} := \frac{I_x + I_y}{2} + \sqrt{\left(\left(\frac{I_x - I_y}{2} \right)^2 + I_{xy}^2 \right)}, I_{min} := \frac{I_x + I_y}{2} - \sqrt{\left(\left(\frac{I_x - I_y}{2} \right)^2 + I_{xy}^2 \right)} \right]$$

$$\#25: \left[I_{max} := 6.286752033 \cdot 10^6, I_{min} := 5.190812996 \cdot 10^5 \right]$$

$$\#26: \left[I_{xp} = I_x \cdot \cos^2(\theta) - 2 \cdot I_{xy} \cdot \cos(\theta) \cdot \sin(\theta) + I_y \cdot \sin^2(\theta), I_{yp} = \right]$$

$$I_y \cdot \cos^2(\theta) + 2 \cdot I_{xy} \cdot \cos(\theta) \cdot \sin(\theta) + I_x \cdot \sin^2(\theta) \Big]$$

$$\#27: \quad \left[I_{xp} = 5.190812996 \cdot 10^5, I_{yp} = 6.286752033 \cdot 10^6 \right]$$

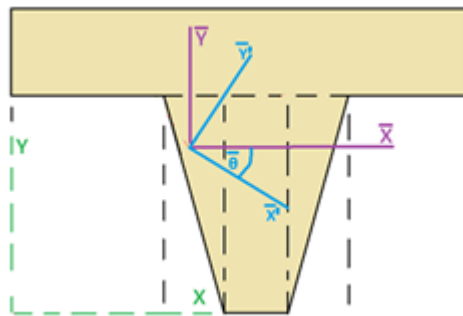
La inercia mayor es alrededor del eje Y' y la inercia menor alrededor del eje X', ambos con giro θ de aproximadamente 33°

Ángulo donde se presentan las inercias principales, respecto a los ejes X e Y centroidales:

$$\#28: \quad \theta_c := \frac{1}{2} \cdot \text{ATAN} \left(- \frac{2 \cdot I_{xyc}}{I_{xc} - I_{yc}} \right)$$

$$\#29: \quad \theta_c := -0.259981302$$

Aproximadamente -15°



$$\#30: \quad \left[I_{maxcg} := \frac{I_{xc} + I_{yc}}{2} + \sqrt{\left(\left(\frac{I_{xc} - I_{yc}}{2} \right)^2 + I_{xyc}^2 \right)}, I_{mincg} := \frac{I_{xc} + I_{yc}}{2} - \sqrt{\left(\left(\frac{I_{xc} - I_{yc}}{2} \right)^2 + I_{xyc}^2 \right)} \right]$$

$$\#31: \quad \left[I_{maxcg} := 7.337181866 \cdot 10^5, I_{mincg} := 2.385966276 \cdot 10^5 \right]$$

$$\#32: \quad \left[I_{xcp} = I_{xc} \cdot \cos^2(\theta_c) - 2 \cdot I_{xyc} \cdot \cos(\theta_c) \cdot \sin(\theta_c) + I_{yc} \cdot \sin^2(\theta_c), I_{ycp} = I_{yc} \cdot \cos^2(\theta_c) + 2 \cdot I_{xyc} \cdot \cos(\theta_c) \cdot \sin(\theta_c) + I_{xc} \cdot \sin^2(\theta_c) \right]$$

$$\#33: \quad \left[I_{xcp} = 2.385966276 \cdot 10^5, I_{ycp} = 7.337181866 \cdot 10^5 \right]$$

La inercia mayor es alrededor del eje Y' centroidal y la inercia menor alrededor del eje X' centroidal, ambos con giro θ de aproximadamente -15°