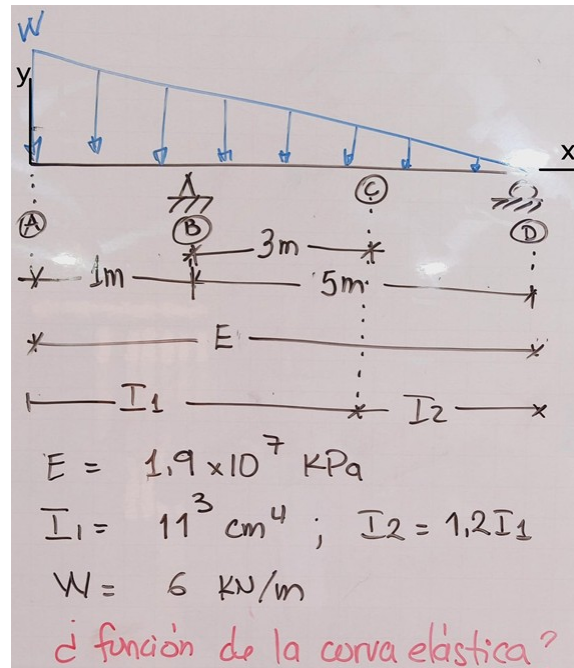




#1: [CaseMode := Sensitive, InputMode := Word]

#2: $[W := 6, E := 1.9 \cdot 10^7, I_1 := 0.11^3, I_2 := 1.2 \cdot I_1]$

#3: $[W := 6, E := 1.9 \cdot 10^7, I_1 := 0.001331, I_2 := 0.0015972]$

Equilibrio estático:

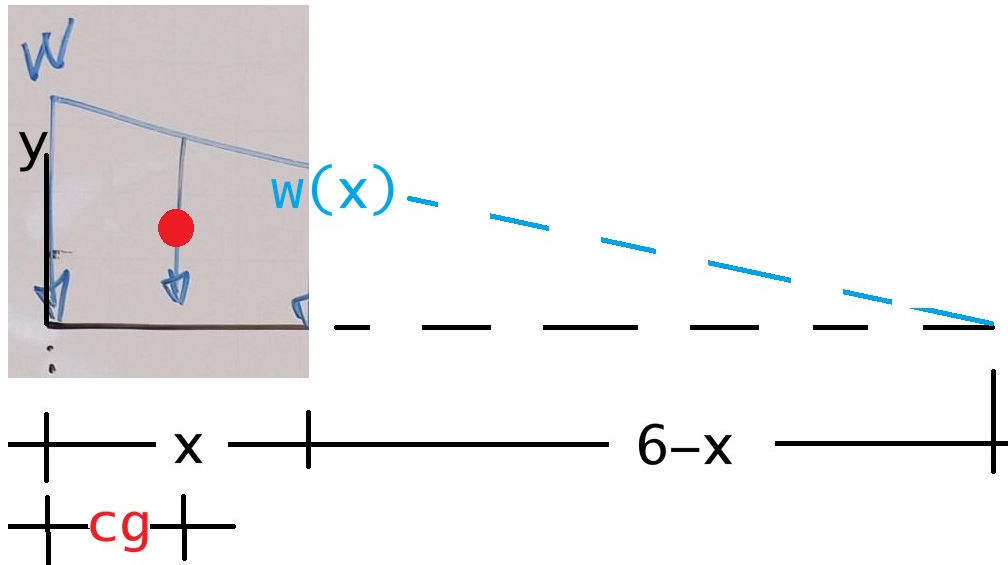
#4: [Rb :=, Rd :=]

#5:
$$\begin{bmatrix} R_b + R_d - \frac{W \cdot 6}{2} = 0 \\ R_b \cdot 1 + R_d \cdot 6 - \frac{W \cdot 6}{2} \cdot \frac{6}{3} = 0 \end{bmatrix}$$

#6: $\left[R_b = \frac{72}{5} \wedge R_d = \frac{18}{5} \right]$

#7: [Rb := 14.4, Rd := 3.6]

Carga y centroide en cualquier punto x:



#8: $[w(x) :=, WT(x) :=, cg(x) :=]$

#9: $\frac{W}{6} = \frac{w(x)}{6 - x}$

#10: $w(x) := \frac{W \cdot (6 - x)}{6}$

#11: $w(x) := 6 - x$

#12: $\left[WT(x) := \frac{W + w(x)}{2} \cdot x, cg(x) := \frac{w(x) \cdot x \cdot \frac{x}{2} + \frac{(W - w(x)) \cdot x}{2} \cdot \frac{x}{3}}{WT(x)} \right]$

#13: $\left[WT(x) := 0.5 \cdot x \cdot (12 - x), cg(x) := \frac{0.666666666666 \cdot x \cdot (x - 9)}{x - 12} \right]$

#14: $\left[WT(x) := \frac{x \cdot (12 - x)}{2}, cg(x) := \frac{2 \cdot x \cdot (x - 9)}{3 \cdot (x - 12)} \right]$

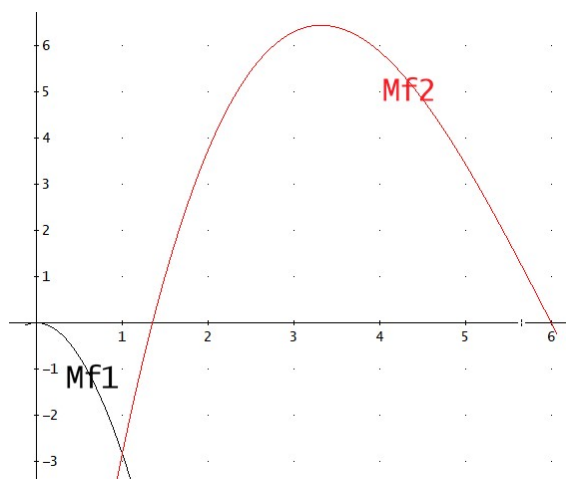
Momentos flectores:

#15: $[Mf1 :=, Mf2 :=]$

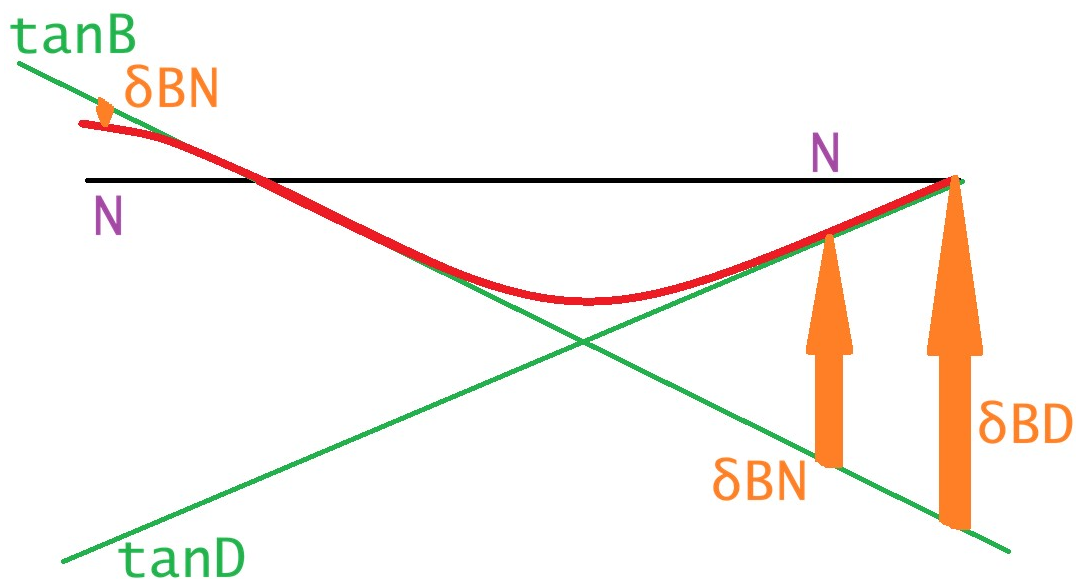
#16: $\left[\begin{array}{l} Mf1 := - WT(x) \cdot (x - cg(x)) \\ Mf2 := - WT(x) \cdot (x - cg(x)) + Rb \cdot (x - 1) \end{array} \right]$

#17:

$$\left[\begin{array}{l} \text{Mf1} := \frac{x^2 \cdot (x - 18)}{6} \\ \text{Mf2} := \frac{5 \cdot x^3 - 90 \cdot x^2 + 432 \cdot x - 432}{30} \end{array} \right]$$



Distancias de la tangente en B y la curva elástica en cualquier punto N o x:



#18: [$\delta\text{BN1} :=$, $\delta\text{BN2} :=$, $\delta\text{BN3} :=$]

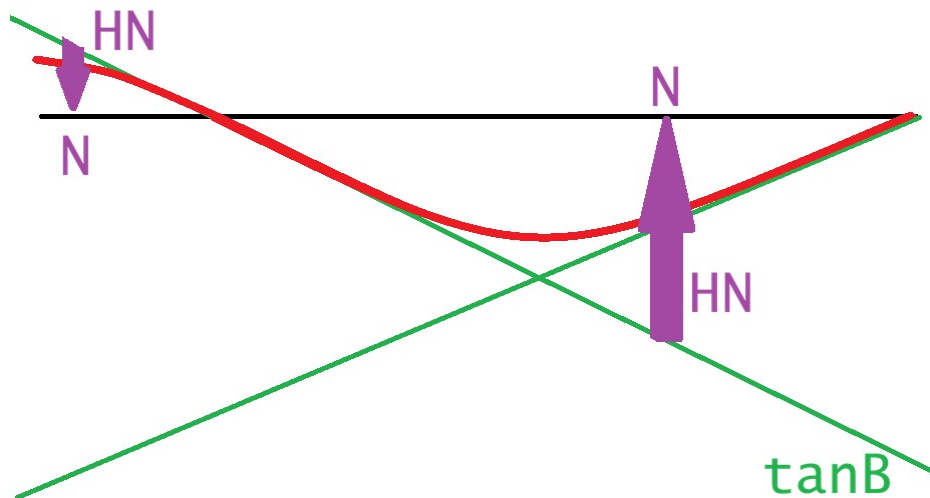
#19:

$$\left[\begin{array}{l} \delta_{BN1} := \frac{1}{E} \cdot \left(\frac{1}{I1} \cdot \int_1^N Mf1 \cdot (N - x) \, dx \right) \\ \delta_{BN2} := \frac{1}{E} \cdot \left(\frac{1}{I1} \cdot \int_1^N Mf2 \cdot (N - x) \, dx \right) \\ \delta_{BN3} := \frac{1}{E} \cdot \left(\frac{1}{I1} \cdot \int_1^4 Mf2 \cdot (N - x) \, dx + \frac{1}{I2} \cdot \int_4^N Mf2 \cdot (N - x) \, dx \right) \end{array} \right]$$

#20:

$$\left[\begin{array}{l} \delta_{BN1} := \frac{N^5 - 30 \cdot N^4 + 115 \cdot N^3 - 86}{3034680} \\ \delta_{BN2} := \frac{N^5 - 30 \cdot N^4 + 288 \cdot N^3 - 864 \cdot N^2 + 979 \cdot N - 374}{3034680} \\ \delta_{BN3} := \frac{5 \cdot N^5 - 150 \cdot N^4 + 1440 \cdot N^3 - 4320 \cdot N^2 + 6386 \cdot N - 6340}{18208080} \end{array} \right]$$

Distancia entre la tangente en B y la viga antes de la deformación en cualquier punto N o x.
 $\delta_{BD} = \delta_{BN3}$ (cuando $N=6$):



#21: $HN :=$

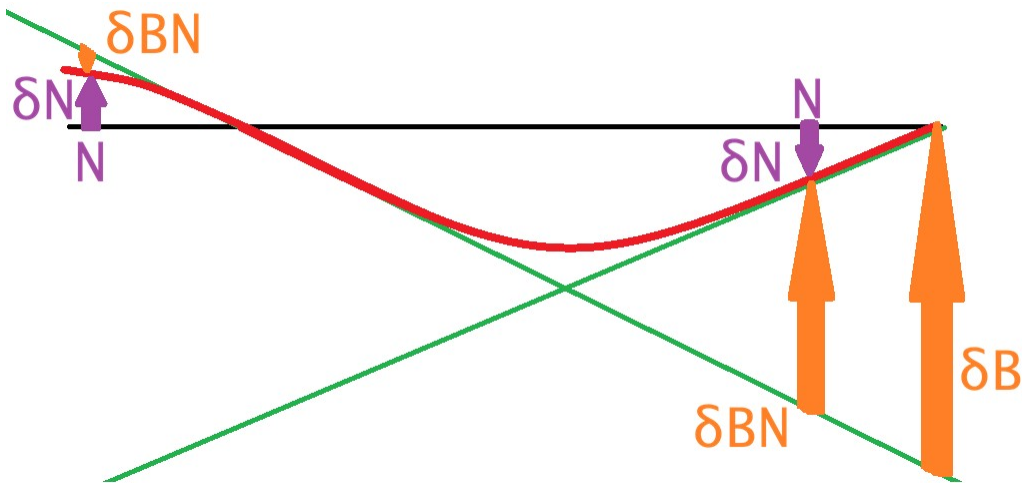
#22: $\delta_{BD} := \text{SUBST}(\delta_{BN3}, [N], [6])$

#23:
$$\delta_{BD} := \frac{3997}{2276010}$$

#24:
$$\frac{\delta_{BD}}{5} = \frac{HN}{N - 1}$$

#25:
$$HN := \frac{3997 \cdot (N - 1)}{11380050}$$

Curva elástica del desplazamiento de cualquier punto N o x de la viga:



#26:
$$[\delta_{N1} :=, \delta_{N2} :=, \delta_{N3} :=]$$

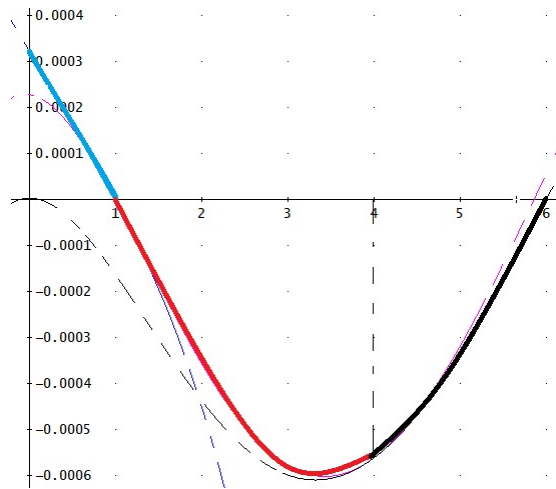
#27:
$$\begin{bmatrix} \delta_{N1} := - (HN - \delta_{BN1}) \\ \delta_{N2} := - (HN - \delta_{BN2}) \\ \delta_{N3} := - (HN - \delta_{BN3}) \end{bmatrix}$$

#28:
$$\begin{bmatrix} \delta_{N1} := 2.196826903 \cdot 10^{-8} \cdot (15 \cdot N^5 - 450 \cdot N^4 - 1.4263 \cdot 10^4 \cdot N + 1.4698 \cdot 10^4) \\ \delta_{N2} := 2.196826903 \cdot 10^{-8} \cdot (15 \cdot N^5 - 450 \cdot N^4 + 4320 \cdot N^3 - 1.296 \cdot 10^4 \cdot N^2 - 1303 \cdot N + 1.0378 \cdot 10^4) \\ \delta_{N3} := 1.098413451 \cdot 10^{-8} \cdot (25 \cdot N^5 - 750 \cdot N^4 + 7200 \cdot N^3 - 2.16 \cdot 10^4 \cdot N^2 - 46 \cdot N + 276) \end{bmatrix}$$

]

#29:

$$\begin{aligned} \delta N1 &:= \frac{15 \cdot N^5 - 450 \cdot N^4 - 14263 \cdot N^3 + 14698}{45520200} \\ \delta N2 &:= \frac{15 \cdot N^5 - 450 \cdot N^4 + 4320 \cdot N^3 - 12960 \cdot N^2 - 1303 \cdot N + 10378}{45520200} \\ \delta N3 &:= \frac{25 \cdot N^5 - 750 \cdot N^4 + 7200 \cdot N^3 - 21600 \cdot N^2 - 46 \cdot N + 276}{91040400} \end{aligned}$$



La

La mayor deformación ocurrirá en $\delta N2$ en $X=4.43m$:

#30: $0 = \frac{d}{dN} \delta N2$

#31: $0 = \frac{75 \cdot N^4 - 1800 \cdot N^3 + 12960 \cdot N^2 - 25920 \cdot N - 1303}{45520200}$

$$\begin{aligned} \#32: \quad N &= 6 - \frac{\sqrt{(4860 - 15 \cdot \sqrt{50565})}}{15} \vee N = \frac{\sqrt{(4860 - 15 \cdot \sqrt{50565})}}{15} + 6 \vee N = 6 - \\ &\frac{\sqrt{(15 \cdot \sqrt{50565} + 4860)}}{15} \vee N = \frac{\sqrt{(15 \cdot \sqrt{50565} + 4860)}}{15} + 6 \end{aligned}$$

$$\#33: \quad N = 8.570776443 \vee N = 3.429223556 \vee N = 12.04905847 \vee N = -0.04905847847$$

La mayor deformación será de 0.6 mm:

$$\#34: \quad \delta N_{2\max} = \text{SUBST}(\delta N_2, N, 3.429223556)$$

$$\#35: \quad \delta N_{2\max} = -0.0006019583697$$